



# Ultrasonic motors with poly phenylene sulfide/alumina/PZT triple-layered vibrators

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## ABSTRACT

Our previously reported ultrasonic motors with poly phenylene sulfide (PPS)/lead zirconate titanate (PZT) double-layered vibrators were capable of providing high rotation speeds and light weight, but their output torques and power were limited owing to the low stiffness of PPS vibrating bodies. In this study, we constructed a triple-layered vibrator by sandwiching a thin alumina disk between the PPS vibrating body and PZT disk to compensate the stiffness. First, their fundamental vibration characteristics were investigated as some of key dimensions were varied. The force factor of the PPS/alumina/PZT triple-layered vibrator reached the maximal value when the neutral axis located at the boundary between the PZT and alumina disks. In contrast, the neutral axes existed in the PZT disks for the PPS/PZT double-layered vibrators; this caused the relatively low force factors compared to the triple-layered vibrators. Subsequently, the load characteristics of the PPS/alumina/PZT triple-layered motors were experimentally assessed. The maximum output torque and power of the triple-layered motors were 5 and 13 times the values of the double-layered motors, respectively, owing to the enhanced force factor and electromechanical coupling factor. Besides, the optimal thickness was lower for the triple- than for the double-layered motor. These advantages indicate the potential of our newly designed triple-layered motors for practical applications.

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## 1. Introduction

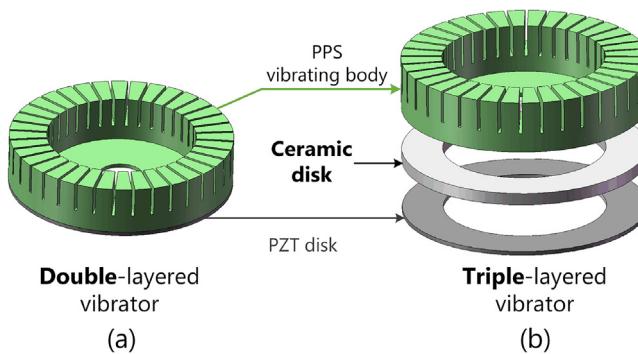
Ultrasonic motors (USMs) exhibit high output torques at low rotational speeds [1,2], simple structures [3], and fast responses [4,5]. Currently, they have some special applications, e.g. auto-focus lenses in digital cameras or optical instruments [6,7]. Recently, USMs capable of working in acid or alkaline environments have become increasingly demanded as potential key actuators of robots for the chemical industry [8,9]. However, the current USMs are inapplicable as most of their vibrators, which are core components of USMs, are made of stainless steel or aluminum alloy. In previous studies [10–15], we bonded vibrating bodies made of poly phenylene sulfide (PPS), a functional polymer with low mechanical loss [10,11], on lead zirconate titanate (PZT) disks to form double-layered motors. They provided high rotation speeds and light weight but limited output torques and power due to the low stiffness of the polymer parts [14]. Utilization of rigid ceramics would be a possible method of enhancing the stiffness [16]. However, our recent study [17] found that the vibrator of which the entire vibrating body was made of rigid ceramics easily frac-

tured even at a low voltage as it exhibited extremely large stress due to the high stiffness. As a consequence, this motor did have the capability to provide a good performance. To overcome these drawbacks, in this study, we develop a new vibrator with a triple-layered structure: A thin disk made of rigid ceramics is sandwiched between the PPS vibrating body and PZT disk; using this structure, the stiffness can be adjusted by changing the dimensions of each layer. To date, several triple-layered (or multi-layered) vibrators for USMs have been reported. Thin films, typically made of nitrides and oxides, were coated on metal vibrating bodies to improve the frictional and/or abrasional properties [18–20]. But these studies did not focus on the vibration characteristics. Actually, the films were too thin to affect the vibration characteristics. Recently, Li et al. have bonded metal/polymer-matrix materials on metal plates to form multi-layered vibrators [21], of which the matrix-material layers have the thicknesses comparable to the metal layers, and analyzed how the material constants and dimensions affect the frictional loss. However, how the motor properties, e.g. the elliptical motion shapes, force factors, and load characteristics, depended on the geometrical parameters were not discussed. It is necessary to systematically investigate these dependences for structural optimization.

In this study, first, we preliminarily select the suitable ceramic(s) as the middle layer by measuring the damping coefficients of

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**Fig. 1.** Schematics of (a) PPS/PZT double-layered and (b) PPS/rigid-ceramic/PZT triple-layered vibrators.

several functional rigid ceramics. Subsequently, we analyze the elliptical motion shapes and the force factors of triple-layered vibrators as the thicknesses of the PPS vibrating bodies and the rigid ceramic layers are varied. Finally, we measure the load characteristics of the motors with triple-layered vibrators. As the first report regarding the PPS/alumina/PZT triple-layered motors, this paper focuses on the load characteristics as they are the fundamental performance for USMs [1,2]. Other performance, such as motion precision, will be explored in our further studies.

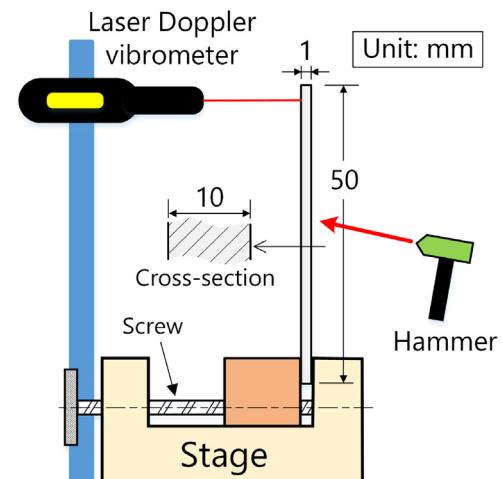
## 2. Triple-layered vibrator

### 2.1. Basic configuration

Fig. 1(a) and (b) illustrate the configurations of the double- and triple-layered vibrators, respectively. In the previous design, a PPS vibrating body with periodical slots is directly bonded on a thin PZT disk. The slotted upper surface contacts the rotor and generate frictional force. The ceramic disk is sandwiched between the PPS vibrating body and the PZT disk in the new design. The three bodies are bonded firmly with epoxy resin to achieve high reliability of this motor. Since the ceramic disk has a simple shape, there exists almost no difference in the structural complexity between the triple- and double-layered vibrators.

### 2.2. Selection of middle layer

To date, there have been no reports regarding the mechanical damping coefficients of rigid ceramics at several tens of kilohertz [10,11]. Thus, prior to evaluation of triple-layered vibrators, the damping coefficients were measured via the impact method to

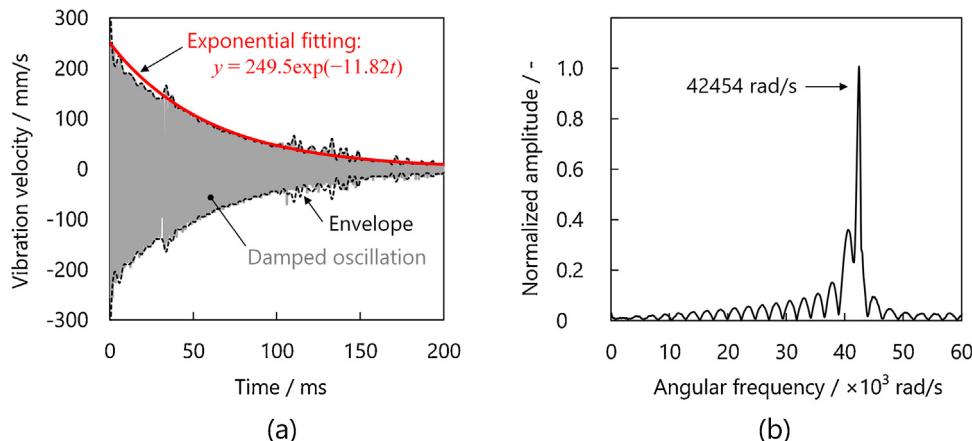


**Fig. 2.** Experimental setup for measuring the damping coefficients of the tested rigid ceramics.

select suitable one(s) as the middle layer [10,12]. Alumina, steatite, silicon carbide, and aluminum nitride are tested as they have wide industrial applications [16]. Their material constants are listed in Table 1. Fig. 2 schematically illustrates the experimental setup. Several rectangular plates 50 mm in length, 10 mm in width, and 1 mm in thickness were prepared, and one end of them was tightly fixed with a screw. We hammered the middle part of the plate to apply an impulse mechanical input, and measured the vibration velocities of the free end with an out-of-plane laser Doppler vibrometer (NLV1232, Polytec, Waldbronn, Germany). The vibration velocity  $y(t)$  is theoretically expressed as

$$y(t) = A \exp(-\beta\omega t) \sin(\omega t + \vartheta), \quad (1)$$

where  $2\beta$ ,  $\omega$ ,  $A$ , and  $\vartheta$  are the damping coefficient, angular frequency, initial amplitude, and phase, respectively. Fig. 3(a) and (b) show the damped oscillation of the alumina plate and an exponential fitting of the envelope, and the response in frequency domain, respectively. The results shown in Fig. 3 demonstrate that  $\beta\omega = 11.82$  and  $\omega = 42,454 \text{ rad/s}$ . Therefore, the damping coefficient  $2\beta$  is 0.0005. For each sample, the damping coefficients are measured for 20 times and the average values are indicated in Fig. 4. Silicon carbide exhibits a damping coefficient of 0.0006, comparable to the value of alumina. However, the silicon carbide samples easily fractured in our experiments; this is assumed to be caused by the fragility [22]. Thus, alumina is employed as the middle layer in our trial.

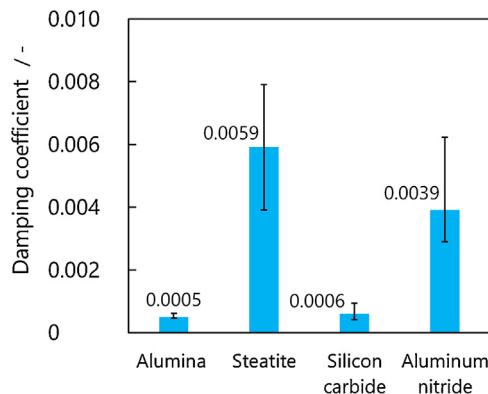


**Fig. 3.** (a) Damped oscillation of alumina plate under an impulse mechanical input and (b) its response in frequency domain.

**Table 1**

Mechanical constants of polymers and ceramics.

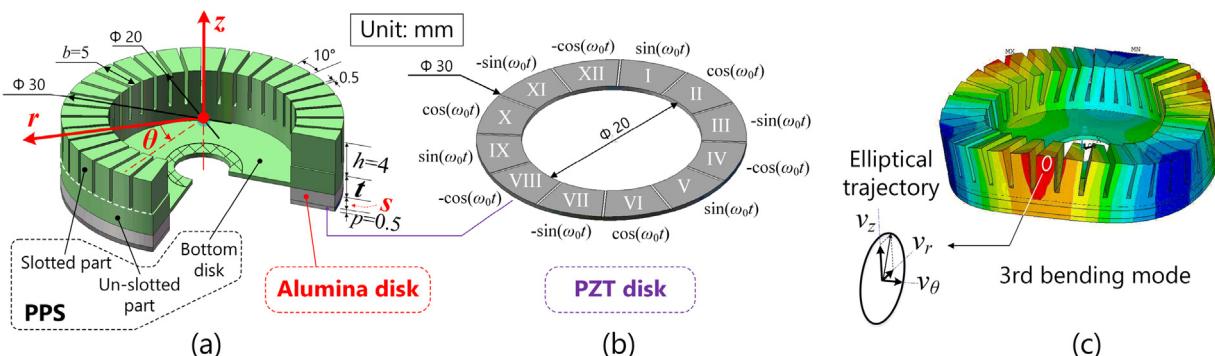
| Materials |   | Density/ $\times 10^3$ kg/m <sup>3</sup> | Elastic modulus/GPa | Poisson's ratio |
|-----------|---|--|---------------------|-----------------|
| Polymer   | PPS   | 1.35                                     | 3.45                | 0.36            |
|           | Alumina ( $\text{Al}_2\text{O}_3$ )                                   | 3.90                                     | 390                 | 0.23            |
| Ceramics  | Stearite ( $3\text{MgO}\cdot 4\text{SiO}_2\cdot \text{H}_2\text{O}$ ) | 2.80                                     | 120                 | 0.22            |
|           | Silicon carbide (SiC)   | 3.10                                     | 410                 | 0.16            |
|           | Aluminum nitride (AlN)  | 3.30                                     | 320                 | 0.24            |

**Fig. 4.** Measured damping coefficients of alumina, steatite, silicon carbide, and aluminum nitride.

### 3. Vibration characteristics of triple-layered vibrators

#### 3.1. Practical design of triple-layered vibrator

**Fig. 5(a)** detailedly illustrates the structure and dimensions of the triple-layered vibrator. The PPS vibrating body had a cylindrical part 20 and 30 mm in inner and outer diameters, respectively, and a bottom disk 0.5 mm in thickness. Radial slots 0.5 mm in width and 4 mm in depth were created on the cylindrical part with an interval of  $10^\circ$ . A polar coordinate ( $z$ ,  $r$ , and  $\theta$  axes) is established on the top surface. The PZT disk (C213, Fuji Ceramics, Fujinomiya, Japan) had inner and outer diameters of 20 and 30 mm, respectively, and a thickness of 0.5 mm. As shown in **Fig. 5(b)**, the bottom surface of the PZT disk was evenly divided into 12 parts (I–XII). The opposite side without division was bonded to one side of the alumina annular disk, of which the inner and outer diameters were respectively identical to those of the PZT disk. The other side of the alumina disk was glued to the bottom surface of the PPS vibrating body. The ceramic disk thickness  $s$  and the un-slotted part thickness  $t$  of the PPS vibrating body are varied in this study.

**Fig. 5.** Triple-layered vibrator. (a) Configuration and dimensions, where  $h$ ,  $t$ ,  $s$ ,  $p$ , and  $b$  represent the height of the slotted part (4 mm), the thickness of the un-slotted part of the PPS vibrating body, the thickness of the alumina disk (0.5 mm), and the radial thickness (5 mm), respectively. (b) the PZT disk and the voltage applied to each electrode. (c) The 3rd bending vibration mode.

#### 3.2. Principle

When sinusoidal voltages  $\sin(\omega_0 t)$ ,  $\cos(\omega_0 t)$ ,  $-\sin(\omega_0 t)$ , and  $-\cos(\omega_0 t)$ , where  $\omega_0$  denotes the resonance frequency, are applied to the electrodes I, V, and IX; II, VI, and X; III, VII, and XI; and IV, VIII, and XII; respectively, as shown in **Fig. 5(b)**, two standing waves in the 3rd bending modes:

$$u_1(t, \theta) = U \sin(\omega_0 t) \sin(k\theta) \quad (2)$$

and

$$u_2(t, \theta) = U \cos(\omega_0 t) \cos(k\theta) \quad (3)$$

are excited. Here,  $\theta$ ,  $U$ , and  $k$  denote the circumferential angle, vibration amplitude, and wave number ( $k = 3$ ), respectively. A traveling wave is formed by the superposition of these standing waves:

$$u_z(t, \theta) = \sum_{i=1}^2 u_i(t, \theta) = U \cos(\omega_0 t - k\theta). \quad (4)$$

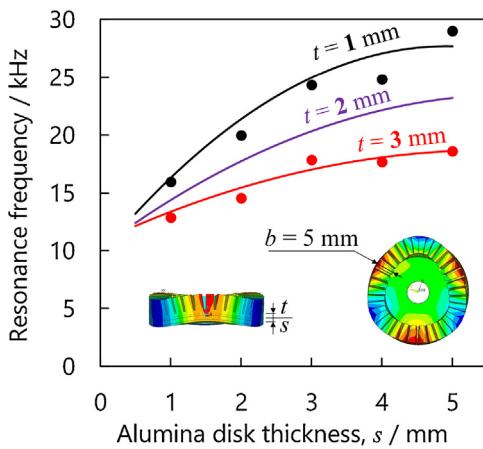
In flexural vibration, the  $\theta$ -axis vibration velocity is derived from  $u_z$ :

$$u_\theta(t, \theta) = -\zeta \cdot \frac{\partial u_z(t, \theta)}{\partial \theta} = \zeta k U \sin(\omega_0 t - k\theta), \quad (5)$$

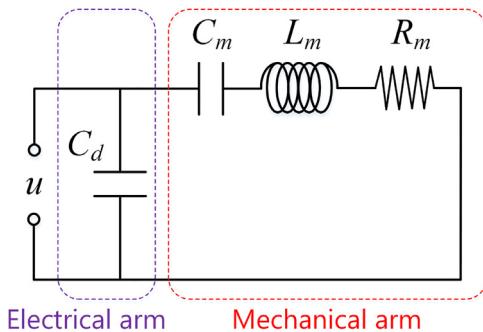
where  $\zeta$  is a ratio determined by the vibrator structure and the vibration mode. Thus,

$$\left[ \frac{u_z(t, \theta)}{U} \right]^2 + \left[ \frac{u_\theta(t, \theta)}{\zeta k U} \right]^2 = 1. \quad (6)$$

The elliptical motion drives the rotor pressed to its upper surface via frictional force. Along the  $r$  axis, there also exist vibration components, which have  $180^\circ$  phase differences with those along the  $z$  axis. Thus, the trajectories in the  $z-r$  planes are lines. The elliptical motion shapes, indicated by the ratios  $v_\theta/v_z$  ( $=\zeta k$ ) and  $v_r/v_z$ , greatly affect the motor performance [1,2,14,15]. Here,  $v_z$  and  $v_r$  are respectively the vertical and radial vibration velocities at anti-nodes, and  $v_\theta$  is the circumferential vibration velocity at nodes. The



**Fig. 6.** Resonance frequencies of the 3rd order bending mode as functions of the thicknesses of alumina disk and un-slotted PPS part. The curves and dots are simulated and experimental results, respectively.



**Fig. 7.** Equivalent circuit model.

other essential indicator is the force factor, defined as the ratio of the current  $i$  to the circumferential vibration velocity  $v_\theta$  [23].

### 3.3. Vibration characteristics

First, through finite element analysis [software: ANSYS (ver. 16.0, ANSYS Inc., Canonsburg, USA)], we investigated the resonance frequencies  $f_r$  of triple-layered vibrators when the alumina disks and the un-slotted parts of PPS vibrating bodies had different thicknesses. As illustrated in Fig. 6, in the cases of the vibrators with 1-mm-thick un-slotted parts, the resonance frequencies increased from 16 to 25 kHz as the ceramic disk thicknesses increased from 1 to 3 mm because of the increased bending stiffness. When the alumina disk was sufficiently thick ( $>3$  mm), the vibrators dominantly exhibited bending vibrations along the  $r$  axis instead of the  $z$  axis, and the resonance frequencies approached the saturated values because they were dominantly determined by the radial thicknesses  $b$  of the PPS un-slotted parts [14]. Besides, the vibrators with identical alumina disk thicknesses showed lower resonance frequencies when the PPS vibrating bodies had thicker un-slotted parts. However, the double-layered vibrators exhibit increases in resonance frequencies as they become thicker [14,24]. Here, a simplified equivalent circuit model [1,23] is introduced to explain the reason.

As illustrated in Fig. 7, an electrical and a mechanical arm are parallelly connected in this model [1,6]. The electrical arm contains the clamped capacitance  $C_d$ , whereas the mechanical arm consists of three serially connected elements, i.e. the equivalent stiffness  $1/C_m$ , mass  $L_m$ , and damper  $R_m$ ; these parameters can be calculated from admittance characteristics [measured with an

impedance analyzer (4294A, Agilent, Santa Clara, CA, USA)] using the following equations:

$$\frac{1}{C_m} = \frac{2\pi f_0 \cdot Q}{Y_{m0}}, \quad (7)$$

$$L_m = \frac{Q}{2\pi f_0 \cdot Y_{m0}}, \quad (8)$$

and

$$R_m = \frac{1}{Y_{m0}}. \quad (9)$$

Here,  $f_0$  represents the resonance frequency,  $Q$  denotes the mechanical quality factor ( $Q=f_0/\Delta f_r$ , where  $\Delta f_r$  represents the bandwidth corresponding to 0.707 times of the maximal vibration amplitude), and  $Y_{m0}$  is the motional admittance. The clamped capacitance equals  $\Delta Y_{nr}/\Delta\omega_{nr}$ , where  $\Delta Y_{nr}$  and  $\Delta\omega_{nr}$  represent the variations in admittance and angular frequency, respectively, in the non-resonant portion of an admittance curve. Table 2 lists the equivalent circuit parameters of the vibrators with  $s = 1$  mm and  $t = 1$  mm (s1t1) as well as  $s = 1$  mm and  $t = 3$  mm (s1t3). The equivalent mass of the s1t3 vibrator is 4 times the value of the s1t1 vibrator because the s1t3 vibrator is thicker. Whereas the equivalent stiffness is twice higher for the s1t3 vibrator than for the s1t1 vibrator. Since the density difference is not large between alumina and PPS, and in the meantime, the un-slotted parts of the PPS vibrating bodies have the thicknesses comparable to the alumina disks, the equivalent mass dominantly depends on their thicknesses. The variation in the equivalent stiffness should be smaller than the change in the equivalent mass because the difference in the elastic moduli between alumina and PPS is larger than that in the densities. In contrast, the double-layered vibrators have increasing resonance frequencies dominantly because their stiffness becomes higher with increasing thickness [14].

Subsequently, we discussed how the elliptical motion shape and the force factor depend on the thicknesses of each layer. Fig. 8(a) demonstrates that the ratios  $v_\theta/v_z$  have negligibly small variations, while the ratios  $v_r/v_z$  exhibit observable variations as the alumina disks became thicker. For instance, the ratios  $v_r/v_z$  of the vibrators with 1-mm-thick PPS un-slotted parts increased gradually in the ranges of 0.5–2.0 mm and 3.5–5.0 mm. However, it sharply increased from 1.0 to 2.5 when the alumina disk thicknesses increased from 2.0 to 3.5 mm. It is assumed to originate from the aforementioned change in the dominant vibration modes. Fig. 8(b) illustrates the variations in force factors against the alumina disk thickness. The vibrators with 1-, 2-, and 3-mm-thick un-slotted parts provided the maximal force factors when the alumina disks had the thicknesses of 0.8, 1.7, and 2.2 mm, respectively. Whereas the force factors of the double-layered vibrators with practical thicknesses ( $<10$  mm) exhibited monotonous enhancements with increasing thickness [14]. This difference can be explained on the basis of the positions of neutral axes on the cross-sections of vibrators.

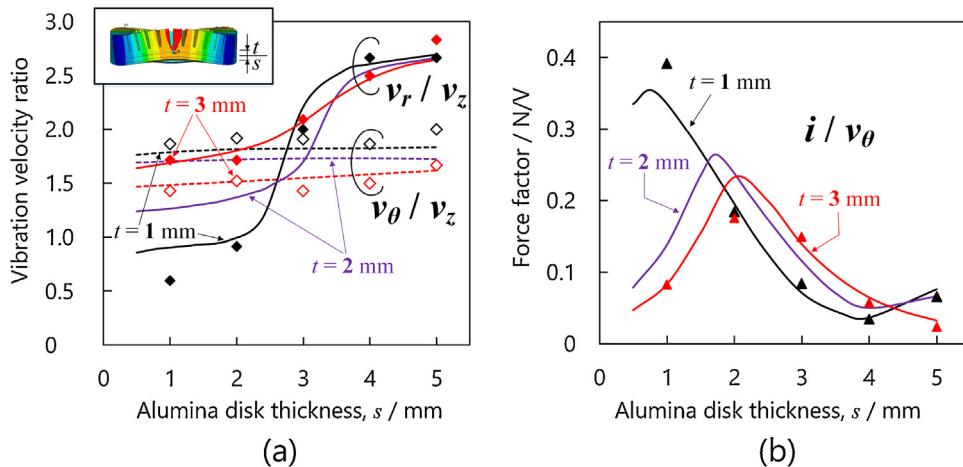
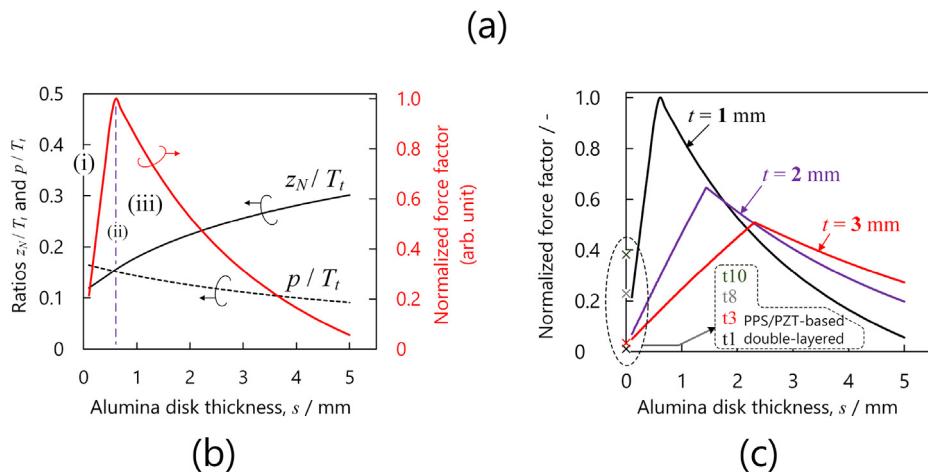
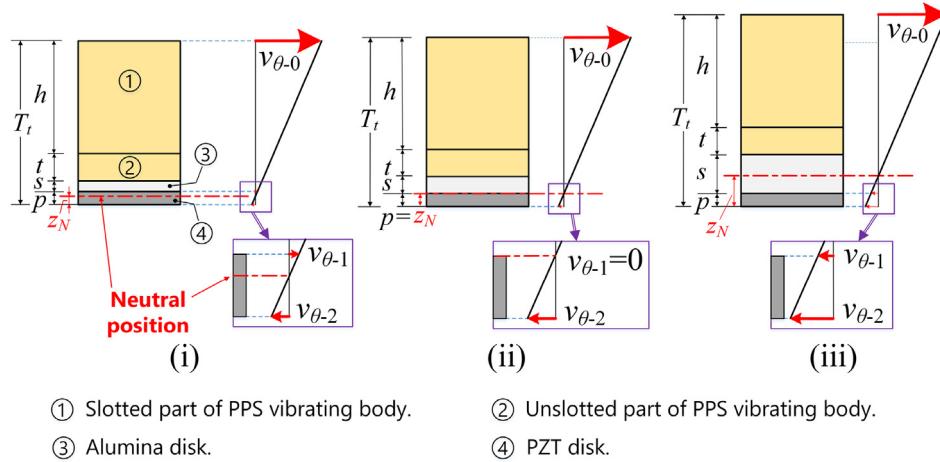
### 3.4. Neutral axis

Fig. 9(a) shows a simplified model for calculating the neutral position. The  $\theta$ -axis vibration velocity equals zero at the neutral position, and increases proportionally to the distance from the neutral position [24]. The neutral axis locates (i) in the PZT disk, (ii) at the boundary between the PZT and alumina disks, and (iii) in the alumina disk when the vibrators have thick, moderate, and thin alumina disks, respectively. In the cases (i) and (iii), the neutral positions  $z_N$  can be respectively obtained by solving the following equations [24]:

**Table 2**

Equivalent circuit parameters of s1t1 and s1t3 vibrators.

| Vibrator | Clamped capacitance, $C_d/\times 10^{-12} \text{ F}$ | Equivalent mass, $L_m/\text{H}$ | Equivalent stiffness, $1/C_m/\times 10^{12} \text{ F}^{-1}$ | Equivalent damper, $R_m/\times 10^3 \Omega$ |
|----------|--|---------------------------------|---|---|
| s1t1     | 6.94   | 43.8                            | 0.435   | 15.0  |
| s1t3     | 6.89   | 158.1                           | 0.974   | 38.7  |

**Fig. 8.** (a) Ratios  $v_\theta/v_z$  and  $v_r/v_z$  and (b) force factors of the vibrators with different thicknesses of alumina disks and un-slotted PPS parts. The curves and dots are simulated and experimental results, respectively.**Fig. 9.** (a) Neutral positions on the vibrators with (i) thin, (ii) moderate, and (iii) thick alumina disks. (b) Ratios  $z_N/T_t$  and  $p/T_t$ , and force factors of the vibrators with 1-mm-thick un-slotted parts. (c) Force factors of the triple-layered vibrators. Here,  $t_1$ ,  $t_3$ ,  $t_8$ , and  $t_{10}$  represent the PPS/PZT double-layered vibrators with 1-, 3-, 8-, and 10-mm-thick un-slotted parts, respectively.

$$E_{PPS} \int_{p-z_N+s}^{p-z_N+s+t+h} zdS + E_{Alu} \int_{p-z_N}^{p-z_N+s} zdS + E_{PCE} \int_0^{p-z_N} zdS + E_{PCE} \int_{-z_N}^0 zdS = 0 \quad (10)$$

and

$$E_{PPS} \int_{s+p-z_N}^{s+p-z_N+t+h} zdS + E_{Alu} \int_0^{s+p-z_N} zdS + E_{Alu} \int_{p-z_N}^0 zdS + E_{PCE} \int_{-z_N}^{p-z_N} zdS = 0, \quad (11)$$

where  $E_{PPS}$ ,  $E_{Alu}$ , and  $E_{PCE}$  denote the elastic moduli of PPS, alumina, and PZT ( $c_{11} = 131$  GPa), respectively, and  $dS$  represents an elementary area ( $=b \cdot dz$ ). The force factor can be estimated as [25]

$$A_f = \frac{e_{31} S_e}{p} \cdot \left| \frac{v_{\theta-1} - v_{\theta-2}}{v_{\theta-0}} \right| = \begin{cases} \frac{e_{31} S_e}{p} \cdot \left| \frac{2z_N - p}{T_t - z_N} \right| & \text{when } z_N \leq p \\ \frac{e_{31} S_e}{p} \cdot \left| \frac{p}{T_t - z_N} \right| & \text{when } z_N > p \end{cases}, \quad (12)$$

where  $v_{\theta-0}$ ,  $v_{\theta-1}$ , and  $v_{\theta-2}$  are respectively the  $\theta$ -axis vibration velocities at the upper surface of the PPS vibrating body, and the upper and bottom surfaces of the PZT disk;  $T_t$  is the total thickness ( $=h+t+s+p$ );  $S_e$  is the electrode area; and  $e_{31}$  is the piezoelectric coefficient.

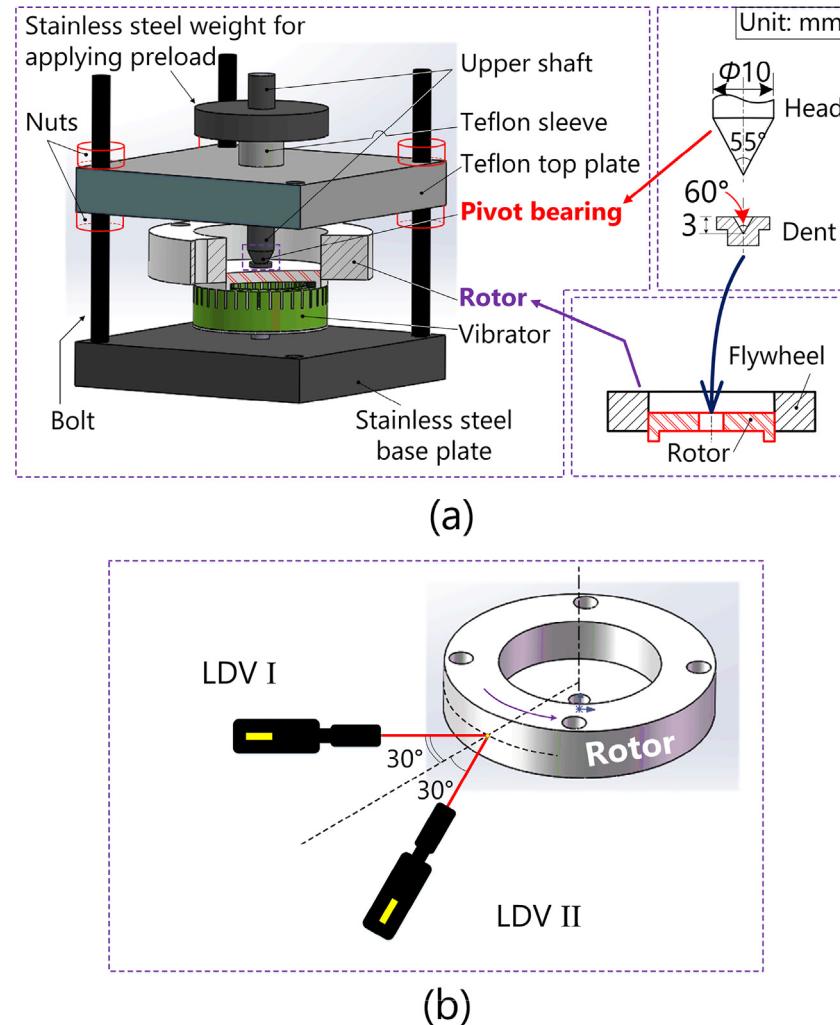
**Fig. 9(b)** plots the ratios  $z_N/T_t$  and  $p/T_t$ , and the force factor as functions of the alumina disk thickness when the PPS vibrating

body has a 1-mm-thick un-slotted part. When the neutral position locates on the PZT disk, its position advances upwards along the  $z$  axis. The force factor becomes higher because the alumina disk exhibits higher stiffness. It reaches the maximal value when the neutral axis is close to the boundary between the PZT and alumina disks. **Fig. 9(c)** illustrates the force factors of other triple-layered vibrators. Clearly, they have almost the same tendencies with the results shown in **Fig. 8(b)**; this validates the effectiveness of this model. The PPS/PZT double-layered vibrators exhibit their neutral axes in PZT disks [similar to the case (a) for triple-layered ones] owing to the relatively high elastic moduli of PZT compared to polymers. Their force factors increase as the PPS vibrating bodies become thicker. It is predictable that double-layered vibrators provide their maximal force factor when their PPS vibrating bodies have sufficient thicknesses. But in the meantime, there exist high vibration components in the radial directions, leading to high frictional loss on the contact surfaces and consequently low performance of motors [14]. **Fig. 9(c)** also demonstrates that, for the double-layered vibrators applicable to USM (<10 mm), the force factors are lower than the values of the triple-layered vibrators.

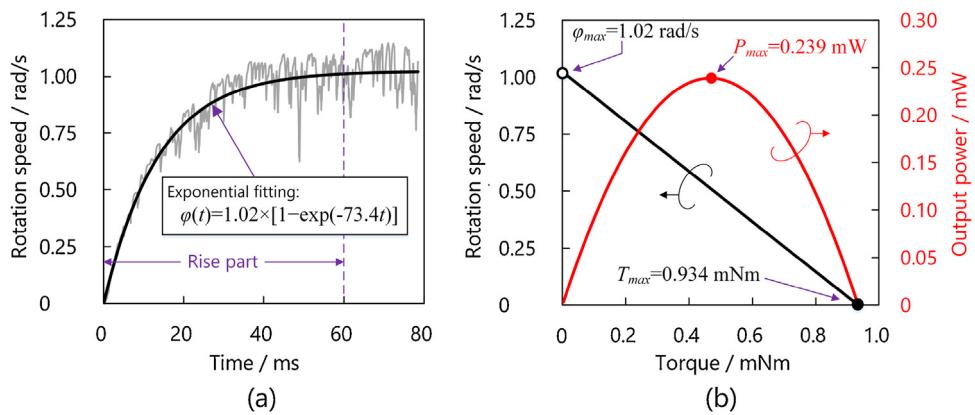
#### 4. Motor performance

##### 4.1. Experimental setup

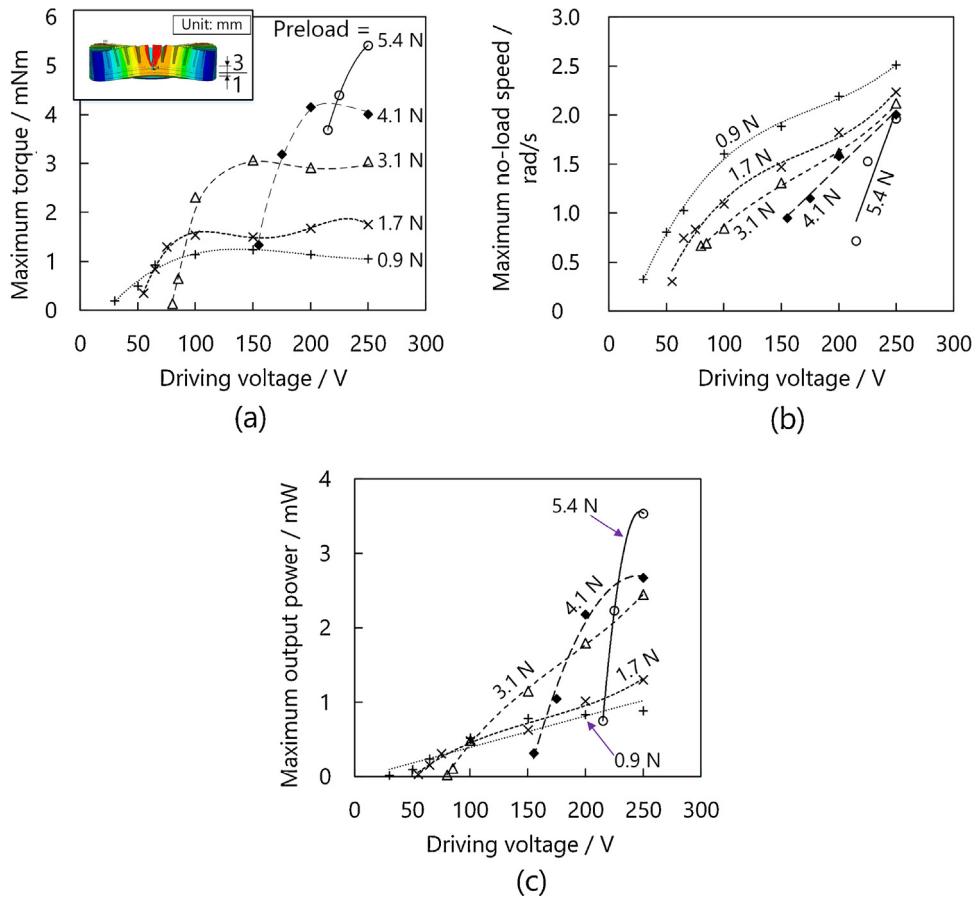
Using the transient method [26], we measured the load characteristics of motors with varying geometrical shapes. **Fig. 10(a)**



**Fig. 10.** (a) Testbed for evaluating motor performance and (b) method of measuring rotation speeds [14,15].



**Fig. 11.** (a) Transient response (grey curve) of rotation speed and its exponential fitting curve (black curve). (b) Load characteristics of the s1t3 motor at 65 V (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article).



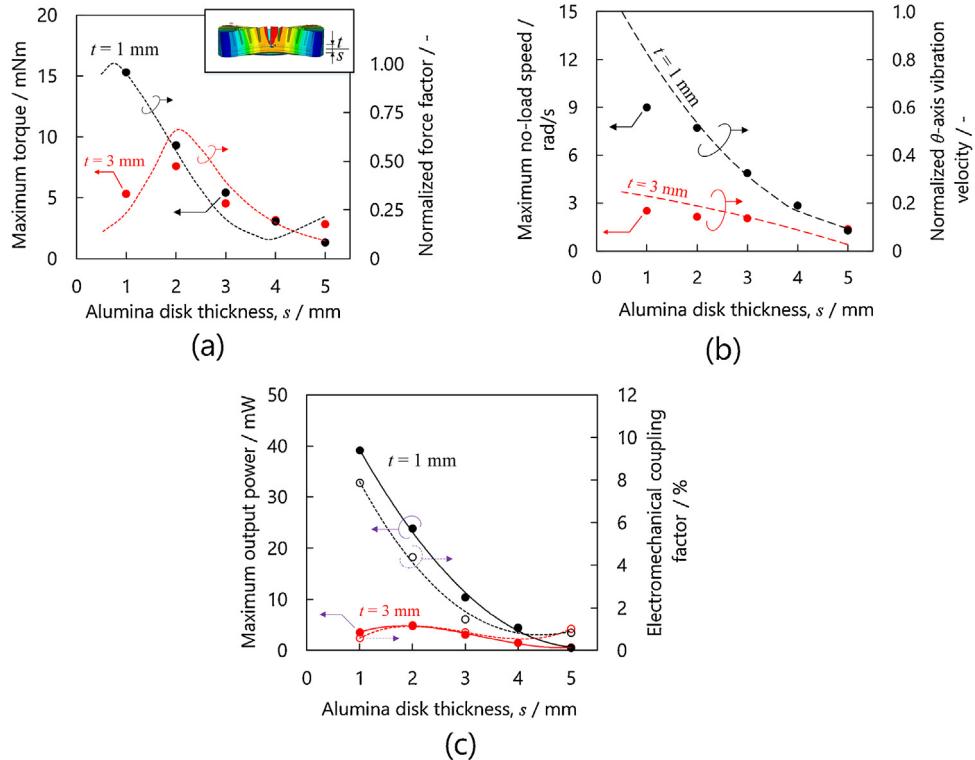
**Fig. 12.** Performance of the s1t3 motor as functions of driving voltages under different preloads: (a) Maximum torque, (b) maximum no-load angular velocity, and (c) maximum output power.

depicts the testbed repeatedly used in our previous studies [14,15]: The vibrator was clamped to a shaft fixed to a stainless-steel base plate. A pivot bearing composed of a conical head and a dent, of which the cone angles were respectively 55° and 60°, was employed to lower the frictional loss. The upper shaft of the bearing was inserted into a sleeve made of Teflon, and the dent was fixed at the center of the rotor. The preload was adjusted by changing the weights applied to the shaft. The transient responses of rotation speeds were measured with two laser Doppler vibrometers: As shown in Fig. 10(b), two beams illuminated the same point on the outer surface of the rotor with the same angles. The rotation speed was obtained from the outputs of these two vibrometers based on a simple geometry [27].

#### 4.2. Case study

Fig. 11(a) showed the transient response of the s1t3 motor when a voltage of 65 V and a preload of 0.9 N were applied. The rotation speed initially exhibited a rapid increase, and at 60 ms, it approached the saturated value of 1.02 rad/s. Since the transient response included high-frequency fluctuations caused by the ultrasonic vibration components, it was fitted with an exponential function:

$$\varphi(t) = \varphi_{max} \cdot [1 - \exp(-\alpha t)], \quad (13)$$



**Fig. 13.** (a) Maximum torques, (b) maximum no-load rotation speeds, and (c) maximum output powers of the motors with different thicknesses of alumina disks and un-slotted PPS parts at 250V and electromechanical coupling factors of the vibrators. The curves in (a) and (b) are simulated results, while those in (c) are fitting curves.

where  $\varphi_{max}$  and  $1/\alpha$  represent the saturated rotation speed and rise time, respectively [25]. The instantaneous output torque and power are expressed as

$$T(t) = J \cdot \frac{d[\varphi(t)]}{dt} \quad (14)$$

and

$$P(t) = J \cdot \frac{d[\varphi(t)]}{dt} \cdot \varphi(t), \quad (15)$$

respectively, where  $J$  denotes the moment of inertia of the flywheel and equals  $1.24 \times 10^{-5}$  kg m<sup>2</sup>. By deleting the time, the rotation speed and output power are presented versus the torque. Fig. 11(b) plots the results. The motor yielded its maximum torque of 0.934 mN m when the rotor started to rotate. At a moderate torque, the motor yielded the maximum output power of 0.239 mW.

Fig. 12(a)–(c) respectively demonstrate the maximum torque, no-load rotation speed, and output power of the s1t3 motor as functions of the driving voltage at different preloads. Dead regions in the torque and no-load speed existed when a low voltage was applied. Initially, the output torque increased proportionally to the voltage, and saturated at a high voltage because it was limited by the frictional force [25]. The rotation speed increased as the voltage became higher. The maximum output power of 3.4 mW was obtained at 250V with the preload of 5.4 N.

#### 4.3. Load characteristics of motors with varying dimensions

Fig. 13 shows the load characteristics of tested motors as functions of the thicknesses of their alumina disks and the PPS un-slotted parts. The applied voltages were set to 250V. As plotted in Fig. 13(a), the maximum torques of the motors with the 1-mm-thick PPS un-slotted parts monotonously decreased from 15 to 2 mN·m as the thickness of alumina disk increased from 1 to 5 mm.

However, among the motors with the 3-mm-thick PPS un-slotted parts, the one with the 2-mm-thick alumina disk yielded a relatively high torque. Clearly, the variations in the maximum torques originates from the changes in the force factors [2,14,28]. Fig. 13(b) illustrates that, because the  $\theta$ -axis vibration velocity decreases as the alumina disk becomes thicker, there exists a reduction in the maximum no-load rotation speed [1,2]. As shown in Fig. 13(c), the electromechanical coupling factor becomes lower with increasing thickness, and leads to the reduction in output power [29]. It is worth mentioning that the s5t1 and s5t3 motors have lower output powers than the s4t1 and s4t3 ones though they have higher electromechanical coupling factors because the negative effects caused by undesirable vibration components offset the positive effects caused by the enhancements in the electromechanical coupling factors [14]. Besides, in the cases of the s5t1 and s5t3 vibrators, bending vibration are dominantly excited on the slotted parts of PPS vibrating bodies rather than the un-slotted parts and alumina disks because the slotted parts have lower bending stiffness [15]; this is assumed to result in the relatively high electromechanical coupling factors of the s5t1 and s5t3 motors compared to those of the s4t1 and s4t3 motors.

Table 3 compares the performance of motors with PPS/alumina/PZT triple-layered vibrators with those with PPS/PZT double-layered vibrators [14]. The maximum torque of the s1t1 motor is 5 times higher than the value of the PPS/PZT motor owing to not only the enhancement in force factors but also the reduction in undesirable vibration components (represented by  $v_r/v_z$ ). More importantly, the maximal thickness is lower for the triple-layered than the double-layered vibrators. The s1t1 motor yields a maximum output power of 39.4 mW, which exceeds 13 times the value of the PPS/PZT motor. Since alumina has lower damper coefficients than polymers, the triple-layered vibrator provides lower mechanical loss (represented as the equivalent damper), which possibly leads to a higher efficiency for the s1t1

**Table 3**

Comparison in performance of USMs with PPS/alumina/PZT triple-layered and PPS/PZT double-layered vibrators.

| Performance  | USM with triple-layered vibrator              | USM with double-layered vibrator |
|--|---|----------------------------------|
| Maximum output torque at 250 V/mNm                                   | 15.2  | 2.9                              |
| Optimal thickness corresponding to maximum output torque/mm          | 2 ( $s = 1 \text{ mm}$ , $t = 1 \text{ mm}$ ) | 8                                |
| Force factor/N·V <sup>-1</sup>                                       | 0.4   | 0.1                              |
| Ratio $v_r/v_z$  | 0.9   | 2.5                              |
| Maximum no-load rotation speed at 250 V/rad s <sup>-1</sup>          | 8.9   | 16.1                             |
| Optimal thickness corresponding to maximum no-load rotation speed/mm | 2   | 2                                |
| Maximum output power at 250 V/mW                                     | 39.1  | 3.0                              |
| Optimal thickness corresponding to maximum output power/mm           | 2   | 2                                |
| Electromechanical coupling factor/%                                  | 7.9   | 0.4                              |
| Maximum efficiency/%   | 8.3   | 4.8                              |
| Equivalent damper/ $\times 10^3 \Omega$                              | 15.0  | 45.0                             |
| Maximum power density/W kg <sup>-1</sup>                             | 10.3  | 2.5                              |

motor than for the double-layered motor. Besides, the weight of the triple-layered motor slightly increases compared to the double-layered one owing to the moderate density of alumina and low thickness of the disk; this causes a higher power density of the PPS/alumina/PZT triple-layered motor.

## 5. Conclusions

In this study, we developed a PPS/alumina/PZT triple-layered vibrator as a core component of USM. After discussing the vibration characteristics of vibrators and measuring the load characteristics of motors, we have drawn the following conclusions:

- (1) The PPS/alumina/PZT triple-layered vibrator exhibited the maximum force factor when its neutral axis was close to the boundary between the PZT and alumina disks.
- (2) Relatively high output torque and power were obtained on the triple-layered motor with the smallest thickness.
- (3) The triple-layered motor exhibited the maximum output torque and power of 15.2 mNm and 39.3 mW, respectively 5 and 13 times the values achieved on our previously reported double-layered motors.

We have gained an understanding on the triple-layered motors and anticipate that the obtained results will provide adequate information for further optimization. To achieve the practical applications in chemical industry, the accessory components of motors, e.g. feeding lines and bearings, will be carefully selected or specially designed in the future.

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